

SUMMARY

Three types of polymer chain length distribution with the random variable N, degree of polymerization

	MPD Polycondensation of α,ω -hydroxyacid	Free radical polymerization with recombination only	POISSON Anionic polymerization by Li-carbanion
n_N , mole fraction of N-mer in discrete form	$p^{N-1}(1-p), 0 < p < 1$ $1 \leq N \leq \infty$	$(N-1)\alpha^{N-2}(1-\alpha)^2, 0 < \alpha < 1$ $2 \leq N \leq \infty$	$\frac{e^{-v} \cdot v^{N-1}}{(N-1)!}, v \gg 1$ $1 \leq N \leq \infty$
N_n , number average degree of polymerization	$\frac{1}{1-p}$	$\frac{2}{1-\alpha}$	$v+1$
w_N , weight fraction of N-mer in discrete form	$N \cdot p^{N-1}(1-p)^2$	$\frac{N(N-1)\alpha^{N-2}(1-\alpha)^3}{2}$	$\frac{N e^{-v} \cdot v^{N-1}}{(v+1)(N-1)!}$
$n(N, p)$, mole fraction of N-mer in the continuous limit	$q \cdot e^{-qN}, q \equiv 1-p$ $0 \leq N \leq \infty$	$\zeta^2 N e^{-\zeta N}, \zeta \equiv 1-\alpha$ $0 \leq N \leq \infty$	$\frac{\exp[-(N-v)^2/2v]}{\sqrt{2\pi v}}$ $0 \leq N \leq \infty$
$g(N, s)$, moments generating function in discrete form	$\sum_{N=1}^{\infty} s^N p^{N-1}(1-p)$ $= \frac{s(1-p)}{(1-ps)}$	$\sum_{N=2}^{\infty} s^N (N-1)\alpha^{N-2} \cdot (1-\alpha)^2$ $= \frac{(1-\alpha)^2 s^2}{(1-\alpha s)^2}$	$\sum_{N=1}^{\infty} s^N \cdot \frac{e^{-v} v^{N-1}}{(N-1)!}$ $= s \cdot \exp[v(s-1)]$
$G(N, s)$, moments generating function in the continuous limit	$\frac{q}{q+s}$	$\frac{\zeta^2}{(\zeta+s)^2}$	$e^{-sv} \cdot e^{s^2 v/2}$
m_k , kth moment	$\frac{k!}{q^k}$	$\frac{(k+1)!}{\zeta^k}$	$\sum_{i=0}^k a_{ki} v^i$ (see below)
$N_w = m_2/m_1$	$\frac{2}{q}$	$\frac{3}{\zeta}$	$\frac{v^2 + v}{v} \equiv v, (v \gg 1)$
$N_z = m_3/m_2$	$\frac{3}{q}$	$\frac{4}{\zeta}$	$\frac{v^3 + 3v^2}{v^2 + v} \equiv v, (v \gg 1)$

$$a_{00}=1, a_{10}=0, a_{11}=1, a_{20}=0, a_{21}=1, a_{22}=1, a_{30}=0, a_{31}=0, a_{32}=3, a_{33}=1,$$

$$a_{40}=0, a_{41}=0, a_{42}=3, a_{43}=6, a_{44}=1, a_{50}=0, a_{51}=0, a_{52}=0, a_{53}=15, a_{54}=10, a_{55}=1$$

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#5-2

